

Geometric Series - Converging or Diverging

$$\sum_{n=3}^{\infty} 5 \left(\frac{2}{3}\right)^{n-1}$$

$$r = \frac{2}{3}$$

$$-1 < r < 1$$

means geometric sequence converges

$$r = \frac{2}{3} \rightarrow -1 < \frac{2}{3} < 1 \quad \therefore \text{converges}$$

$$\frac{a}{1-r} \quad 5 \left(\frac{2}{3}\right)^{3-1} = \frac{20}{9} \rightarrow a$$

$$\frac{20/9}{1 - \frac{2}{3}} = \frac{20/9}{\frac{3}{3} - \frac{2}{3}} = \frac{20}{9}$$

$$\sum_{n=1}^{\infty} \frac{\pi^n}{3^{n+2}} = \sum_{n=1}^{\infty} \frac{\pi^n}{3^n \cdot 3^2} = \frac{1}{9} \sum_{n=1}^{\infty} \frac{\pi^n}{3^n} = \frac{1}{9} \sum_{n=1}^{\infty} \left(\frac{\pi}{3}\right)^n$$

$$r = \frac{\pi}{3}$$

$$\frac{\pi}{3} > 1 \quad -1 < r < 1$$

\therefore diverging